

Locked modes and magnetic field errors in the Madison Symmetric Torus

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In the Madison Symmetric Torus (MST) reversed-field pinch [Fusion Technol. **19**, 131 (1991)] magnetic oscillations become stationary (locked) in the lab frame as a result of a process involving interactions between the modes, sawteeth, and field errors. Several helical modes become phase locked to each other to form a rotating localized disturbance, the disturbance locks to an impulsive field error generated at a sawtooth crash, the error fields grow monotonically after locking (perhaps due to an unstable interaction between the modes and field error), and over tens of milliseconds of growth confinement degrades and the discharge eventually terminates. Field error control has been partially successful in eliminating locking.

I. INTRODUCTION

Long-wavelength, global magnetic oscillations greatly influence macroscopic behavior of reversed-field pinch (RFP) and tokamak plasmas. Such oscillations, usually identified as magnetohydrodynamic (MHD) tearing modes, can cause sawtooth oscillations and major disruptions. These modes are sensitive to the structure of the equilibrium magnetic field. Ordinarily they rotate with respect to the lab frame. However, in the presence of a non-axisymmetric error in the equilibrium magnetic field the modes can cease rotation and become stationary or "locked" in the lab frame. In recent years, many studies of locked modes in tokamaks have illustrated their deleterious effects on plasma behavior.¹⁻⁵

In the Madison Symmetric Torus (MST) reversed-field pinch locked modes occur in response to field errors, with similarities to locking in tokamaks.⁵⁻⁷ However, the locking in MST is part of a rich process, which includes interactions between helical modes, field errors, and sawteeth. We view this wall locking process as a sequence of the following observed events.

(1) *Phase locking between modes.* The dominant modes in MST (with poloidal and toroidal mode numbers $m=1$, $n=5-10$) become locked in phase to form a rotating, localized, magnetic disturbance with a toroidal width of about one-fourth the circumference. This is similar to earlier observations of phase locking in the Ohmically Heated Toroidal Experiment (OHTE)⁸ and TPE1-RM15⁹ devices, as well as in MHD computation.^{10,11}

(2) *Impulsive field error generated by sawtooth crash.* The sawtooth crash flattens the current density profile and shifts the plasma inward, generating a sudden radial field error at the poloidal gap in the shell.

(3) *Rotating modes lock to field error.* Coincident with the sawtooth crash (and impulsive field error), the rotating, phase-locked structure halts at the location of the field error (poloidal gap).

(4) *Field errors grow after locking.* After locking, stationary helical modes are formed and magnetic field error at both the poloidal and toroidal gaps begin to grow. The growth, roughly linear in time, is interpreted as arising

from an unstable interaction between the helical modes and the field error at the toroidal gap.

(5) *Confinement degrades and discharge terminates prematurely.* As the field errors grow for tens of milliseconds, confinement degrades, eventually terminating the discharge.

The modes do not lock at every sawtooth crash, but when they do, this sequence is extremely reproducible and obviously harmful to plasma confinement. Each step in the process is described below. After describing the apparatus in Sec. II, we discuss the observations of mode-mode locking (Sec. III), mode locking to the wall (Sec. IV), field error growth after locking (Sec. V), and partial control of the locking by field error control (Sec. VI). We summarize in Sec. VII.

II. DESCRIPTION OF APPARATUS

A. MST device and plasma parameters

MST is a large toroidal reversed-field pinch, which, from a field error point of view, contains three unique design features.¹² First, the toroidal magnetic field is produced by driving poloidal current through the conducting vacuum vessel (5 cm thick aluminum, minor radius=0.52 m, major radius=1.5 m). This single-turn coil design produces a very low field ripple in vacuum. The dominant spatial Fourier component (poloidal mode number $m=0$, toroidal mode number $n=4$) has an amplitude of 0.5% of the toroidal field. Second, the poloidal magnetic field windings do not encircle the torus axisymmetrically, but are wrapped about the iron core. Third, vacuum pumping is provided through 193, 1½ in. diam holes in the lower half of the chamber, which are spread over nearly the entire toroidal circumference. The resulting field error is a small ripple of small spatial scale, as opposed to an error of large radial extent that would accompany a large porthole. The conducting shell contains two insulated voltage gaps. One cut, the toroidal gap, extends the long way around to allow application of the toroidal magnetic field. The poloidal gap extends the short way around the shell to allow the pulsed poloidal magnetic field to enter the shell.

TABLE I. Limiting values of plasma parameters achieved on MST.

I_p	<	0.6 MA
Vl	>	12 V
τ_{pulse}	<	80 msec
$T_{e(0)}$		50–430 eV
$n_{e(0)}$		$0.75\text{--}3 \times 10^{13} \text{ cm}^{-3}$
T_i	<	350 eV
β_p		4%–17%

MST discharges, formed in the self-reversal mode, have been produced for durations up to 80 msec and plasma currents up to 0.6 MA. MST can operate over the range of plasma parameters depicted in Table I.

B. Sources of field errors

The dominant source of field error in MST is the poloidal gap in the vacuum shell. This gap interrupts the flow of toroidal current in the shell surface. This current is an image of the plasma current and must be accurately controlled at the gap. A small poloidal component of the current at the gap can produce a significant radial magnetic field that enters the shell through the 1 cm wide gap. Such errors generally have low m values and a very broad range of n values, since the gap is localized toroidally. Hence, these errors are usually resonant with the equilibrium field in the plasma. The error at the toroidal gap is enhanced in the presence of plasma; however, the errors are generally not resonant in the plasma and are less deleterious than the other gap.

The errors generated at the poloidal gap can be divided into four categories according to their time dependence. The first type has the same time waveform as the plasma current and results from the poloidal field winding being imperfectly placed for the specific plasma equilibrium. The dominant poloidal mode numbers of this error are $m=0\text{--}2$. The second field error begins a slow growth later in time (at about 10–20 msec) and is caused by the finite electrical resistivity of the shell. It is dominantly an $m=4$ error related to the rectangular symmetry of the poloidal field winding. The third type is an oscillatory $m=1$ error generated by the rotating helical modes. The fourth type is an impulsive $m=1$ error generated by the sudden equilibrium inward shift that accompanies the crash phase of a sawtooth oscillation.

The poloidal gap is instrumented with two sets of correction coils (saddle coils) to reduce the first two types of field errors. Current in the first set of correction coils is driven in series with the poloidal field winding to produce a correction proportional to the plasma current. A radial field of the first type penetrating the gap is thereby reduced to 1% of the equilibrium field. The second set is driven by a simple waveshaping circuit to match the slowly varying error of the second type. The third and the fourth type of error occurs on a submillisecond time scale and, at present, are not corrected. Unfortunately, the fourth type of field error plays an important role in mode locking to the wall.

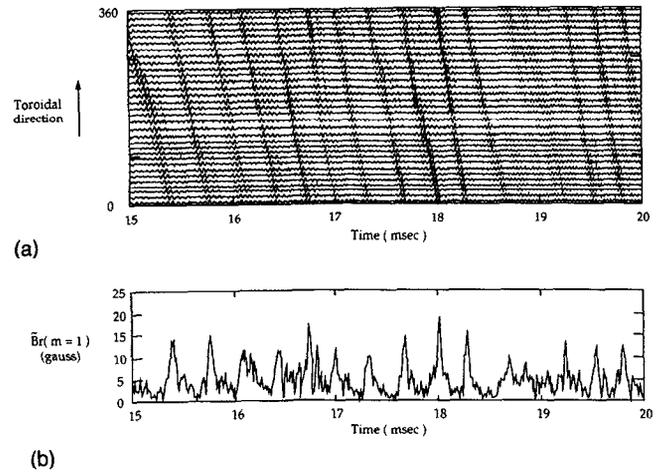


FIG. 1. The coupling between the helical tearing modes and the error fields in MST is illustrated. (a) The poloidal magnetic field fluctuation at 32 toroidal locations plotted in their toroidal order as a function of time. This plot shows the toroidal extent, toroidal speed, and direction of the localized structure. This is a case in which the toroidal structure is highly localized with a broad modal content ($n=6\text{--}10$). Around 19 msec, the toroidal structure is less localized as fewer number of modes are present. (b) The amplitude of the $m=1$ component of the magnetic field error at the poloidal gap for the same time window as in part (a). The $m=1$ amplitude is enhanced as the localized structure crosses the poloidal gap (at zero toroidal angle).

C. Magnetic diagnostics

About 400 magnetic pickup coils are attached to the inside surface of the vacuum shell to diagnose the magnetic fluctuations and gap field errors. The helical modes have also been diagnosed by other methods, such as soft x-ray emission,¹³ which will not be described here. To measure the field errors, 32 coils are distributed around the poloidal gap, and 16 coils are distributed around the toroidal gap. These coils detect the radial magnetic field at the gaps, with mode numbers up to $m=16$ at the poloidal gap and mode numbers up to $n=8$ at the toroidal gap. To measure the toroidal mode spectrum, coils are located at 64 toroidal locations, equally spaced, with three orthogonal coils at each location (for each directional component). Another set of 16, three-axis coils is distributed poloidally to measure the poloidal mode spectrum. Thus, magnetic fluctuations can be detected with mode numbers up to $m=8$ and $n=32$. The signals are typically amplified with a 250 kHz bandwidth and digitized up to a 1 MHz sampling rate.

III. MODE-MODE PHASE LOCKING

Magnetic fluctuations in MST are dominated by low-frequency components (10–30 kHz), which contain about 90% of the power.^{14–16} These fluctuations, identified as tearing modes, are composed of several spatial modes with $m=1$, $n=5\text{--}10$. Typically these modes phase lock to each other and constructively interfere to produce a rotating, toroidally localized disturbance. The localization and rotation is clear in Fig. 1(a), which displays the time dependence of \bar{B} at 32 different toroidal locations. Usually the disturbance extends over about one-fourth of the toroidal circumference and rotates in the ion diamagnetic direction

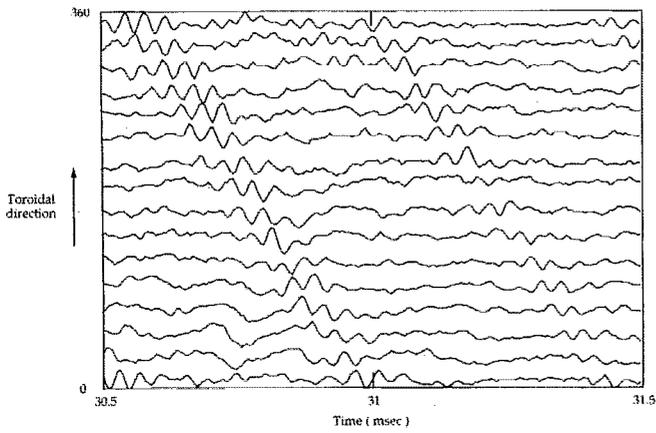


FIG. 2. The field error at the toroidal gap at 16 toroidal locations plotted in their toroidal order versus time. This plot shows a rotating, localized error correlated with the rotating tearing modes. This error results from the interruption of the poloidal shell current at the gap.

at about 10^6 cm/sec. However, the speed, and even the direction, can vary with time, depending on the modal content of the spectrum. The phase locking between modes is a result of nonlinear coupling, as has been identified through bispectral analysis of magnetic fluctuations in MST.¹⁷

The rotating disturbance produces a field error at both gaps (of the third type described in Sec. II B). The poloidal field windings are distributed for axisymmetric shell image currents corresponding to a particular plasma equilibrium. The tearing modes produce helical image currents in the shell. The mismatch between the winding distribution and image currents yields a radial field at the poloidal gap as the rotating disturbance passes the gap. This is illustrated in Fig. 1(b). The field error at the gap is an $m=1$ component, as expected, since it is generated by the $m=1$ modes. Similarly, the rotating disturbance induces a localized error field at the toroidal gap, shown in Fig. 2.

MST and other RFP experiments displays vivid sawtooth oscillations.¹⁸ The data described above correspond to times during the rise phase of a sawtooth. At the crash, the magnetic fluctuation spectrum broadens drastically ($n > 32$), and the spectrum cannot be accurately resolved. After the crash, the toroidal spectrum is composed of only $n=5-7$, with $n=5$ being typically the dominant mode. The localized structure slowly reforms as the other low-frequency modes ($n=6-10$) begin to grow and the $n=5$ mode decays. Eventually the dominant modes phase lock to produce a highly localized structure that remains localized until the following sawtooth event. This cycle, displayed in Fig. 3, repeats throughout the discharge. Occasionally the $n=5-7$ modes become locked to the wall at the crash and remain stationary for the remainder of the discharge with the same modal content.

IV. MODE LOCKING TO THE WALL

A sawtooth crash generates an impulsive field error at the poloidal gap (of the fourth type described in Sec. II B).

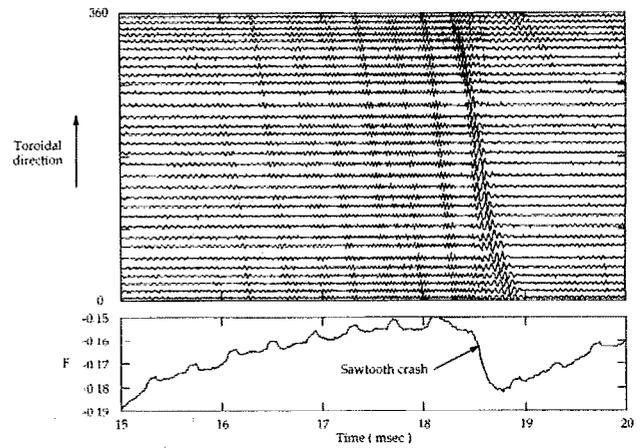


FIG. 3. The poloidal magnetic field at 32 toroidal locations versus time, and the field reversal parameter, F , for one sawtooth cycle. The spectrum starts narrow, where only few modes are present ($n=5-7$), resulting in a broad disturbance. Thereafter the spectrum broadens ($n=6-10$) and forms a localized toroidal structure until the following sawtooth crash. After the crash, the spectrum is narrow and the dominant mode is $n=5$.

The current density profile flattens during a sawtooth crash. This is indicated in measurements of the edge poloidal current density (which is roughly parallel to the magnetic field) in the edge plasma, shown in Fig. 4, with a small Rogowskii coil. At a crash the current density doubles, while the total plasma current remains unchanged. The current flattening shifts the plasma inward, as indicated by the decrease in the edge poloidal magnetic field asymmetry factor given by $B_\theta = B_0(1 + \epsilon\Lambda \cos \theta)$, as shown in Fig. 5(a). As a result of the sudden change in the equilibrium, the poloidal field windings become mismatched, and an impulsive $m=1$ radial field error is produced, as shown in Fig. 5(b).

At the time of a sawtooth crash, the helical modes sometimes cease rotation and the localized structure remains at the location of the poloidal gap for the remainder of the discharge, as shown in Fig. 6. The locking of the disturbance is observed in the toroidal coil array. The toroidal angle at which the mode locks corresponds to the poloidal gap, and the time of locking corresponds to the sawtooth crash. This locking of the mode to the wall re-

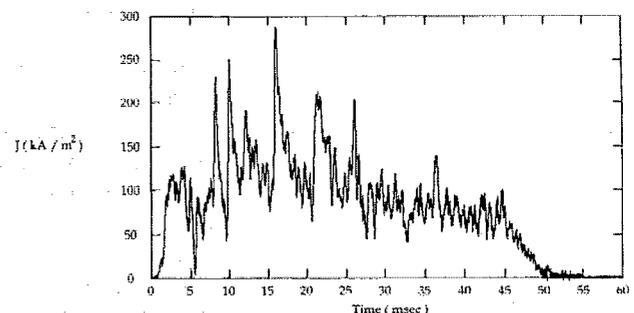


FIG. 4. The poloidal current density at the edge of the plasma versus time. The sawtooth crash causes the current density to double at the edge, while the total plasma current remains constant.

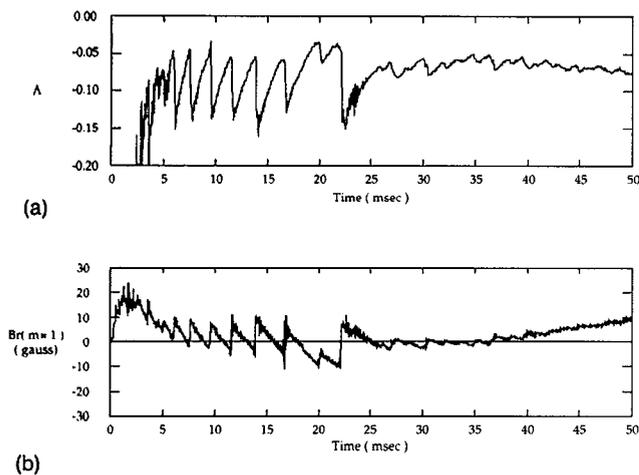


FIG. 5. This plot demonstrates the coupling between the sawtooth and the generation of the impulsive error field that causes the rotating modes to lock. (a) The poloidal asymmetry factor Λ versus time. Here Λ decreases at the sawtooth crash, showing the flattening and inward shift of the plasma current channel. The change in Λ is due mostly to the change in the internal inductance not a change of poloidal beta, which would require beta to triple its value. (b) The $m=1$ component of the magnetic field error of the poloidal gap. Showing an increase in the $m=1$ component correlated with the change in Λ .

sults from the interaction between the mode and the impulsive magnetic field error at the poloidal gap. The detailed mechanism for locking (e.g., viscous damping, impurity generation from enhanced plasma-wall interaction, or magnetic boundary conditions) has not been determined. The locking substantially alters the discharge evolution and leads to early termination, as seen in Fig. 7.

V. FIELD ERROR GROWTH AFTER LOCKING TO THE WALL

After the helical modes lock to the wall, they remain locked and large until discharge termination. This is in contrast to the usual case, where the modes do not lock and reset to zero at each crash. In Fig. 8 we show the time evolution of the dominant Fourier modes, $n=5-7$. The modes become stationary at 11 msec. The stationary modes are also evident as a growing field error. At the poloidal

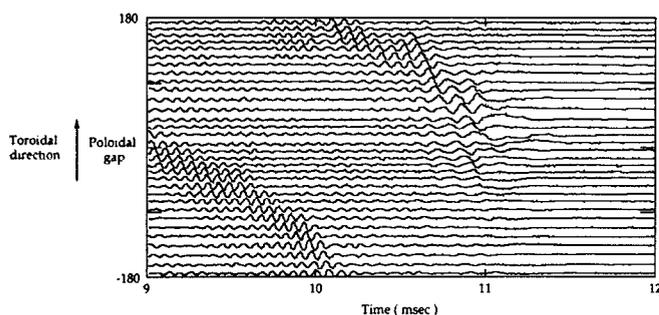


FIG. 6. The poloidal magnetic field fluctuation at 32 toroidal locations versus time, showing the locking at the poloidal gap at about 11 msec.

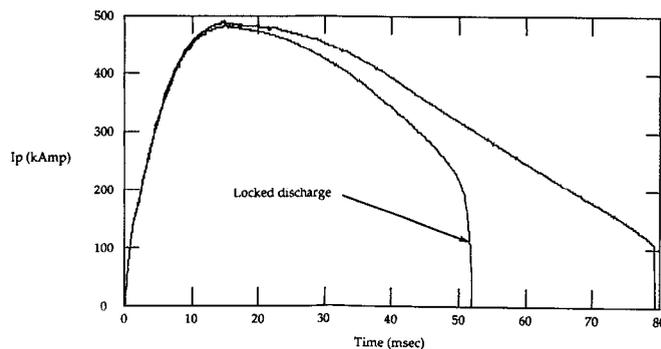


FIG. 7. The plasma current for two identical discharges, except that one discharge is locked and the other is not. The locked discharge is degraded.

gap a growing $m=1$ error is observed, and at the toroidal gap the growing error consists of $n=5-7$ modes, as seen in Fig. 9.

The growth of the field errors at the gaps after the toroidal modes become stationary might arise from an instability generated from the interaction of the helical mode with the toroidal gap. Such a "field error instability" was predicted in a heuristic model by Kerst. A helical plasma current (such as produced by a tearing mode) will induce a radial magnetic field at the toroidal gap with the same toroidal mode number as the tearing mode. As the radial magnetic field enters the plasma it diverges spatially, producing a toroidal magnetic field perturbation, δB_r . The resulting Lorentz force, $J_p \times \delta B_r$, produces a radial force pushing the initial helical distortion toward the toroidal gap, unstably enhancing the original perturbation.

Consider a plasma current column in a large aspect ratio toroidal shell with a minor radius, r_0 , major radius, R , and wall thickness, d , all in units of cm. Let the shell have one toroidal gap located at the inner midplane of width, G , in cm. If the current is displaced vertically with toroidal modulation of $y=y_0 \sin(n\varnothing)$, where y_0 is the vertical displacement, in cm, then the radial field, δB_r , in Gauss, generated at the toroidal gap, is given by

$$\delta B_r(\varnothing) = 0.4\pi \left(\frac{y_0 I}{2\pi r_0 d} \right) \sin(n\varnothing),$$

where I is the plasma current.

If we assume that this flux fills the volume of the torus, then a toroidal field perturbation, δB_\varnothing , will be produced,

$$\delta B_\varnothing(\varnothing) = 0.2 \left(\frac{y_0 I R G}{\pi d n r_0^3} \right) \cos(n\varnothing).$$

The total radial force on the current I toward the toroidal gap due to its transverse undulation across δB_r is then given by

$$F = \frac{I^2 G y_0^2 R}{10 r_0^3 n d},$$

and the restoring force resulting from the conducting wall is given by

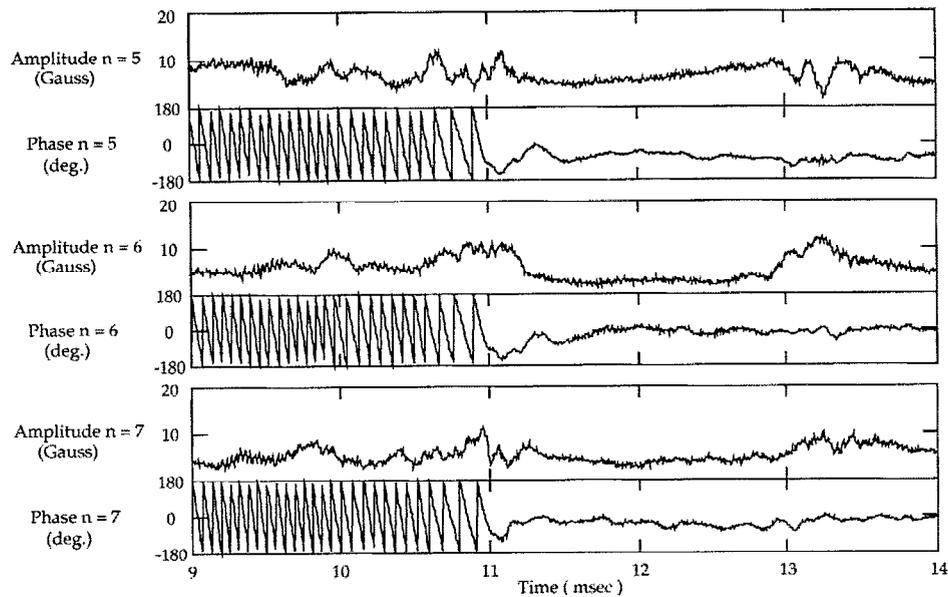


FIG. 8. The amplitudes and phases of the $n=5-7$ tearing modes. The modes lock around 11 msec. The amplitudes are about the same as when the modes are rotating. In all cases the spectrum is narrow after a sawtooth crash ($n=5-7$). When the modes are locked, only $n=5-7$ are ever large.

$$F_r = \frac{\pi R}{n} \left(\frac{0.2 I^2 y_0}{r_0^2} \right).$$

The ratio of the perturbation force, F , to the restoring force, F_r is

$$\frac{F}{F_r} = \frac{G y_0}{2\pi r_0 d} < \frac{G}{2\pi d} = 4\% \quad (\text{for MST}).$$

These forces are present throughout the discharge. However, if the modes are stationary, the image currents in the shell resistively decay, and the restoring force is reduced. At the same time, the column moves closer to the gap, and the effective gap width, G , increases, and the effective wall thickness, d , reduces, thereby enhancing the driving force.

The equivalent vertical magnetic field, B_v , that would produce the same radial force toward the toroidal gap, is given by

$$B_v \leq \frac{B_p}{2\pi} \left(\frac{G}{d} \right).$$

This vertical field is observed as an increasing error field at the poloidal gap as the factor G/d increases.

VI. CONTROL OF LOCKING TO THE WALL

Since the locking is believed to be caused by the impulsive field error at the poloidal gap during the sawtooth crash, control of locking is possible through field error control. This is quite difficult, since such control would require feedback of the magnetic field at the gap on the submillisecond time scale of the crash. However, we have been able to eliminate the locking in some discharges by imposing a steady $m=1$ radial field at the gap in the direction opposite to the impulsive error. Although the steady field increases the field error at times other than during the crash, it diminishes the error during the crash. As a result the impulsive error is reduced to a level at which locking does not occur, as illustrated in Fig. 10. In MST locking is most prevalent at high plasma current (400–600 kA). The effectiveness of the offset error diminishes with current. At the highest currents locking is often unavoidable. Presumably, if the sawtooth oscillations are eliminated, then locking would not occur. It is anticipated that improved flat topping of the discharge might eliminate inductive contributions to the current density profile to form a more sawtooth-stable discharge.

VII. DISCUSSION

A process has been observed in MST that culminates with the monotonic growth of a locked mode, which eventually terminates the discharge. The locking of tearing modes in MST has obvious similarities to locked modes in

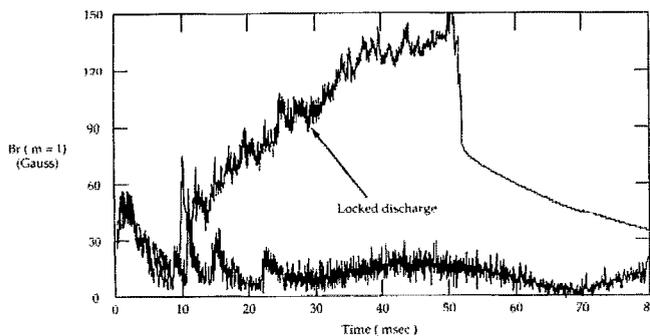


FIG. 9. The $m=1$ component of the magnetic field error at the poloidal gap for two identical discharges, except that one discharge is locked and the other is not. Once the modes lock, the $m=1$ field error starts to grow to large values, eventually terminating the discharge.

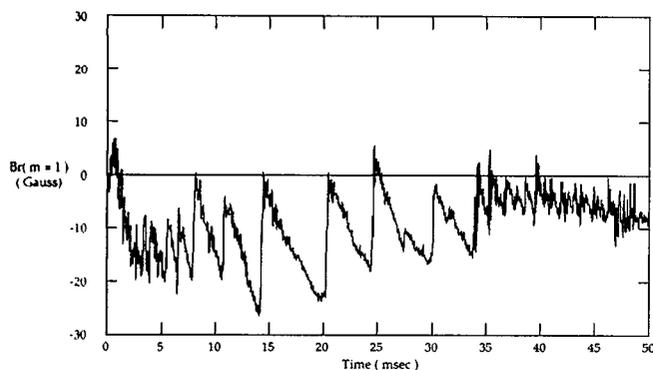


FIG. 10. The $m=1$ component of the magnetic field error at the poloidal gap with a negative offset. The offset is to prevent the sawtooth crash from driving the impulsive field error, $m=1$, to a large positive value. This was found to be successful in preventing locked discharges [compare with Fig. 5(b)].

tokamaks. In both cases, locked modes can occur at any time during the discharge (current rise or flattop), can be caused by field errors, can be initiated by a sawtooth crash, and lead to degraded confinement. One difference is that locked modes in tokamaks can unlock during a discharge, whereas in MST the modes remain locked until termination.

However, the helical modes, sawteeth, and field errors couple in MST in ways not reported in tokamaks. First, in tokamaks locked modes usually are composed of only one helical mode. In RFP's several tearing modes are present simultaneously and become phase locked, as a result of nonlinear mode coupling. In most tokamaks the field error is a dc preexisting error, whereas in MST it is generated by the sawtooth crash (which is itself likely caused by the phase-locked tearing modes). The sawtooth-generated impulsive field error then causes the rotating modes to lock to the field error. Unlike tokamak locked modes, after locking in MST the error fields grow monotonically, perhaps for 10–30 msec, eventually terminating the discharge. We conjecture the growth after locking is generated by an unstable interaction between the field error and the helical mode (a "field error instability").

Locked modes are a detriment to confinement. Two possible means to eliminate locking are to suppress the field errors or to eliminate sawteeth. We have applied a steady field opposite to the impulsive error. As a result of this offsetting field, the impulsive errors are diminished and locking is sometimes eliminated. However, it is more desirable to eliminate the sawtooth oscillations, the source of the impulsive field error. MST displays strong sawteeth in nearly all plasmas, in contrast to other RFP's, which are sawtooth dominated only at high values of the pinch parameter. A possible reason is that the current in MST is not sufficiently time independent during the discharge, and inductive effects produce a current density profile more prone to sawteeth. The MST power supplies are being

modified for an improved flattop to test this speculation. On the positive side, the sensitivity of tearing modes to the magnetic field boundary conditions suggests the possibility of controlling the modes through edge control.

ACKNOWLEDGMENT

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